

Correction: Savoir factoriser (identités remarquables).

Exemple 1 Développer et réduire les expressions suivantes:

1. $a^2 - b^2 = (a - b)(a + b).$

(a) $x^2 - 9y^2 = x^2 - (3y)^2 = (x - 3y)(x + 3y).$

(b) $(x + 3)^2 - (2x - 5)^2 = [(x + 3) - (2x - 5)][(x + 3) + (2x - 5)] = (-x + 8)(3x - 2).$

(c) $(x - 5)(2x - 6) - (x^2 - 25) = (x - 5)(2x - 6) - (x - 5)(x + 5) = (x - 5)[(2x - 6) - (x + 5)] = (x - 5)(x - 11)$

(d) $(x - 3)^2(3x + 2) + 2x(x^2 - 9) = (x - 3)^2(3x + 2) + 2x(x - 3)(x + 3) = (x - 3)[(x - 3)(3x + 2) + 2x(x + 3)] = (x - 3)(3x^2 + 2x - 9x - 6 + 2x^2 + 6x) = (x - 3)(5x^2 - x - 6)$

2. $a^2 + 2ab + b^2 = (a + b)^2.$

(a) $x^2 + 10x + 25 = (x + 5)^2$

(b) $4x^2 + 20x + 25 = (2x + 5)^2$

(c) $(x + 1)(2x - 6) - (x^2 + 2x + 1) = (x + 1)(2x - 6) - (x + 1)^2 = (x + 1)[(2x - 6) - (x + 1)] = (x + 1)(x - 7)$

(d) $(x + 3)(3x + 2) + 2(x^2 + 6x + 9) = (x + 3)(3x + 2) + 2(x + 3)^2 = (x + 3)[(3x + 2) + 2(x + 3)] = (x + 3)(5x + 8)$